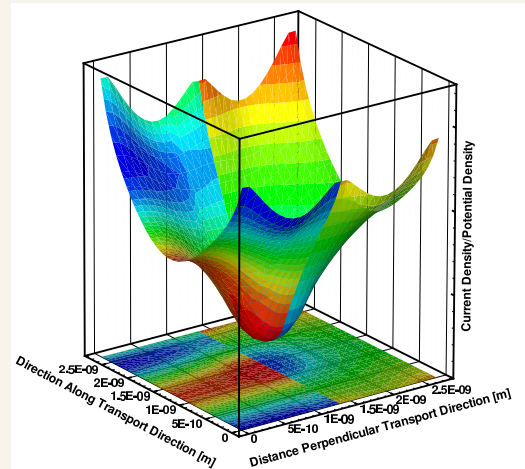


# Quantum Simulation of Nanocrystalline Composite Thermoelectric Properties:

*InterPACK Conference 2009*



*T.D. Musho<sup>1</sup> D.G. Walker<sup>2</sup>*

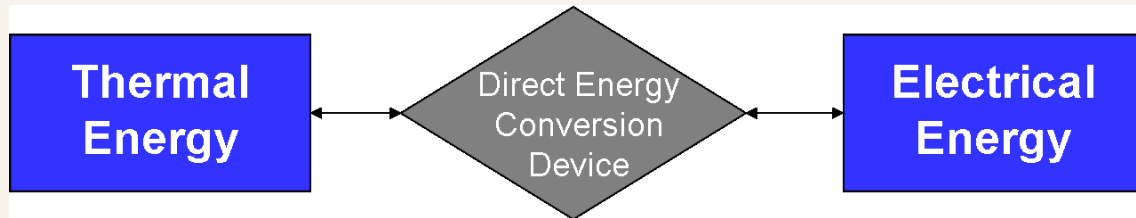
*<sup>1</sup> Department of Material Science, Vanderbilt University, Nashville, Tennessee*

*<sup>2</sup> Department of Mechanical Engineering, Vanderbilt University, Nashville, Tennessee*

*Sponsor: NSF*

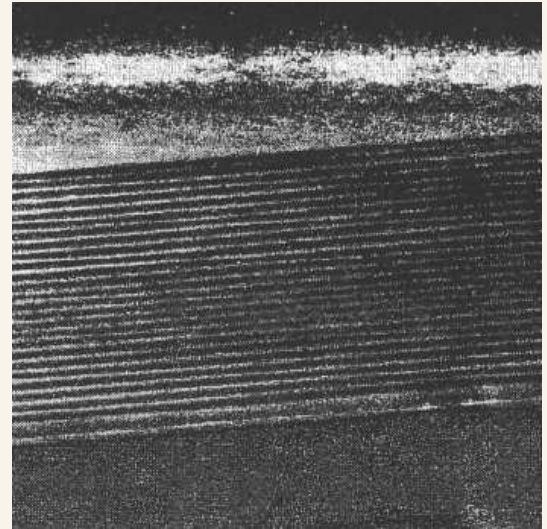
*July 23, 2009*

- Direct Energy Conversion Devices
  - Thermoelectrics ( $>1$  ZT)
  - Electric Cooler
- Nanostructured Material
  - Atom-by-Atom Basis
  - Quantum Confinement
- Wave Based Model
  - Quantum Mechanical Effects
  - Schrodinger-Poisson Solver
- Items of Interest
  - Electrical Transport
  - Device Trends
  - Optimal Device Spatial Parameters
    - \* Crystal Diameter
    - \* Crystal Spacing
  - Matrix and Crystal Material

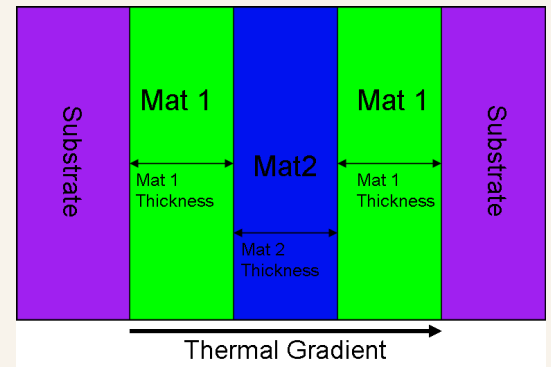
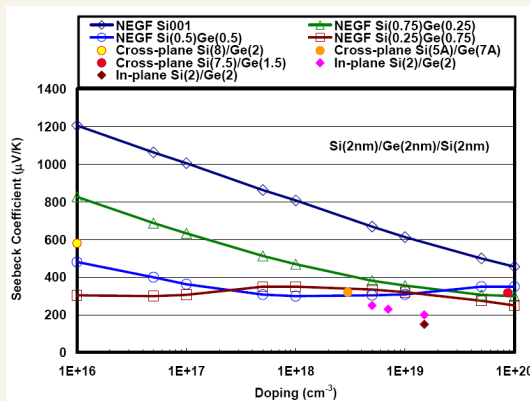




- Non-Equilibrium Green's Function (NEGF) Method
- Superlattice Structure
  - 1d Heterostructure, Silicon-Germanium junction
- Electrical Transport
  - Quantum Confinement
  - Tunneling Effects
  - Increased Density of States (DOS)



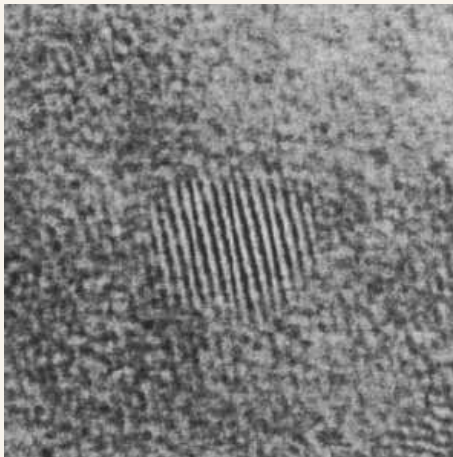
Nozik, Annu. Rev. Phys. Chem. 2001. 52:193231



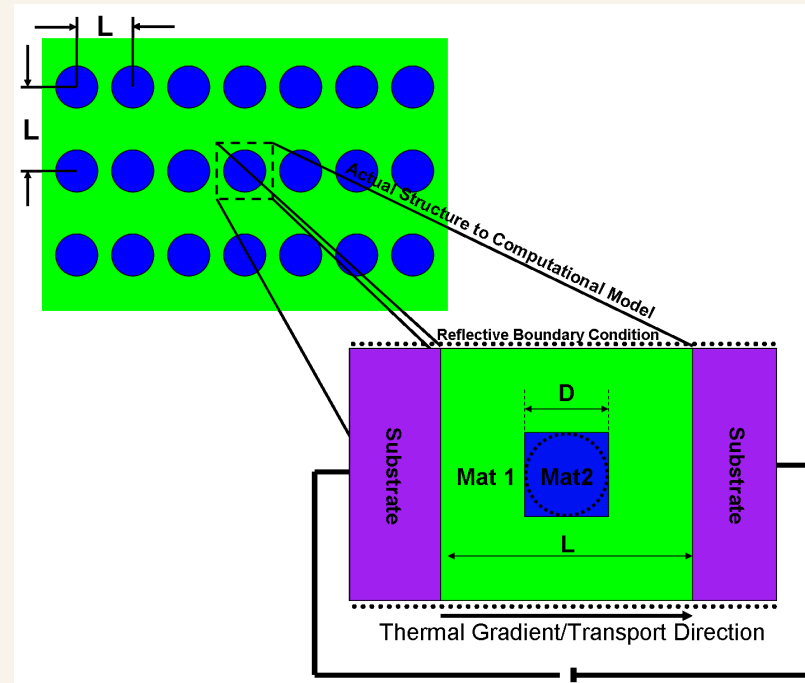
# Nanocrystalline Composite



- Nanostructure
  - 2d Heterostructure,  
Silicon-Germanium junction
- Electrical Transport
  - Quantum Confinement
  - Planar Transport
  - Increased Surface to Volume



Nozik, Annu. Rev. Phys. Chem. 2001. 52:193231



# Band Structure

- Straining of Crystal
  - Difference in lattice constant
  - Deformation Potential
- Silicon-Germanium Structure
  - Crystal Material Strained

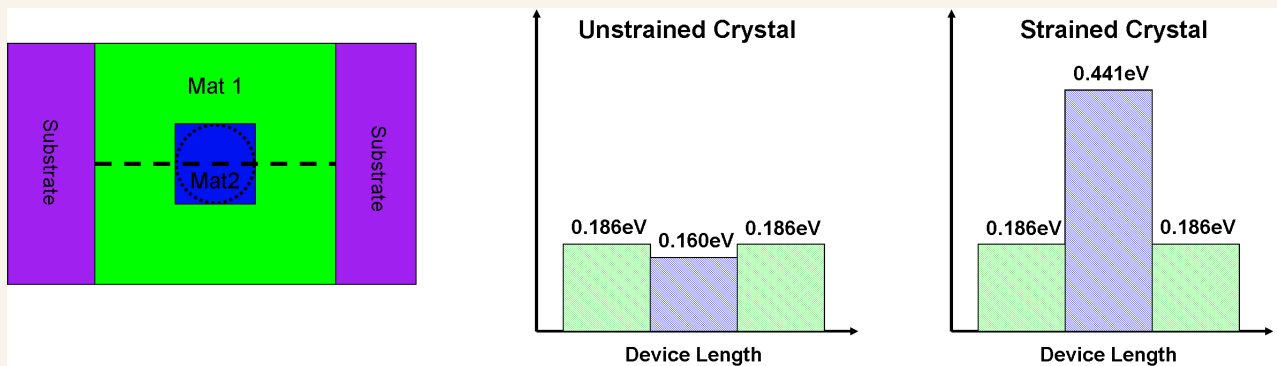
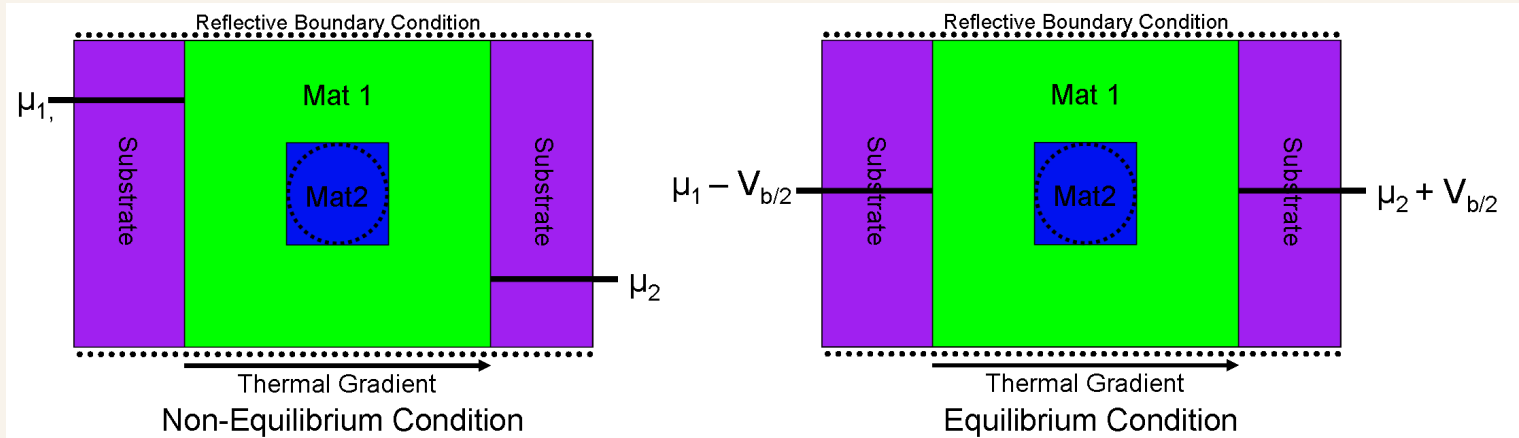
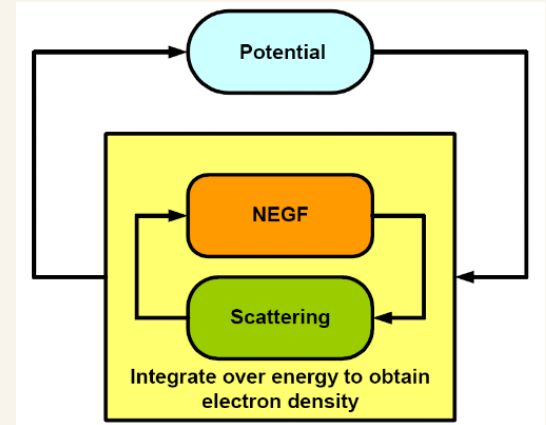


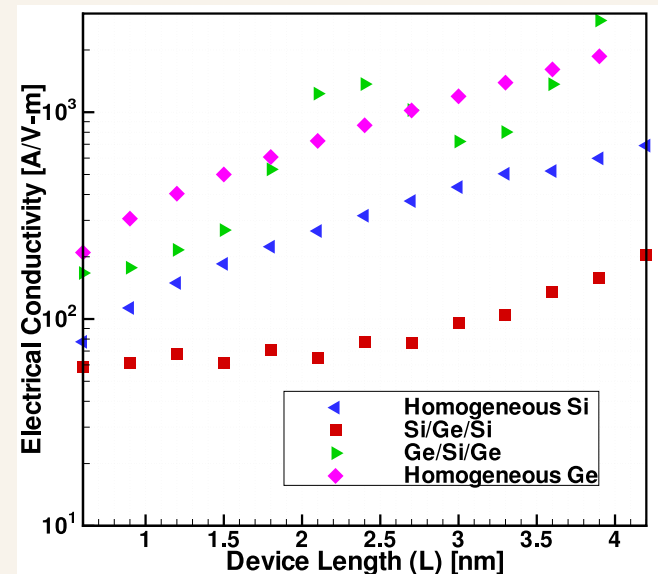
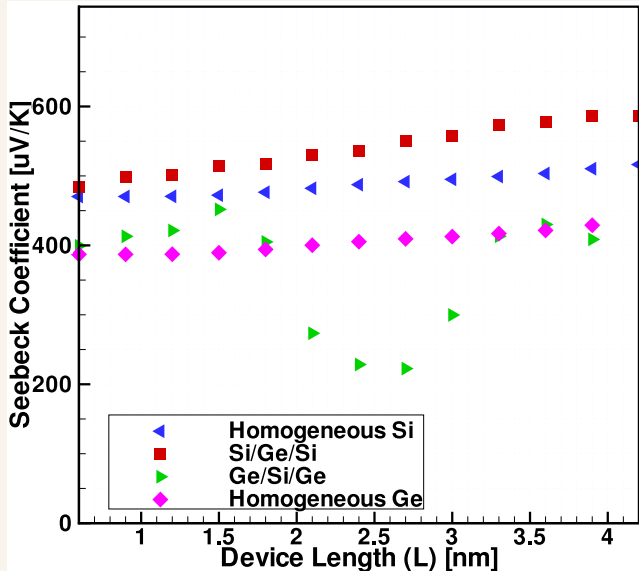
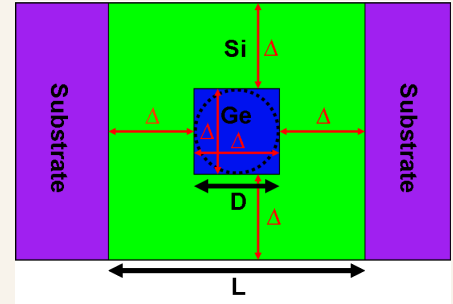
Table 1: Conduction Band Edge with Strain ( $E_f = 0.1$ )

Device	Mat1 $E_c$ [eV]	Mat2 $E_c$ [eV]
Si-Ge	0.186	0.602
Ge-Si	0.160	-0.266
Si-Si	0.186	0.186
Ge-Ge	0.160	0.160

- Wave Based Model
  - Non-Equilibrium Green's Function (NEGF) Method
  - Self Consistent Schrodinger-Poisson Solver
- 2d Effective Mass Hamiltonian
- 2d Spatially Varying Dielectric Potential
- Ballistic Transport



- Increased Diameter of Crystal and Spacing Proportionally.  $D = L/3$

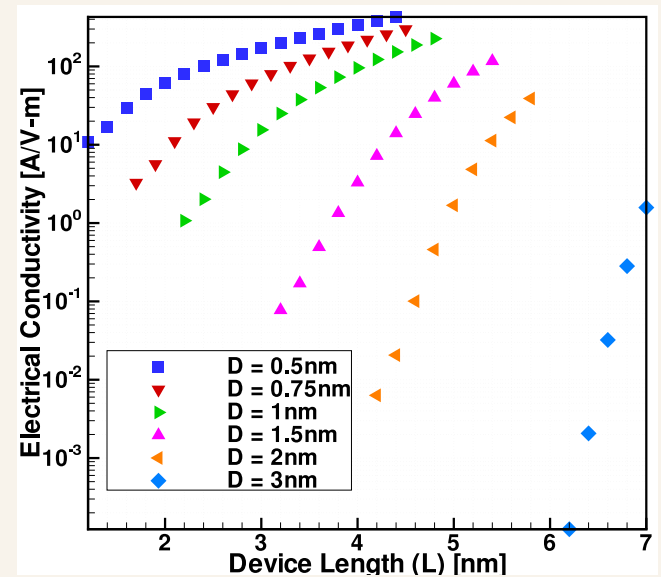
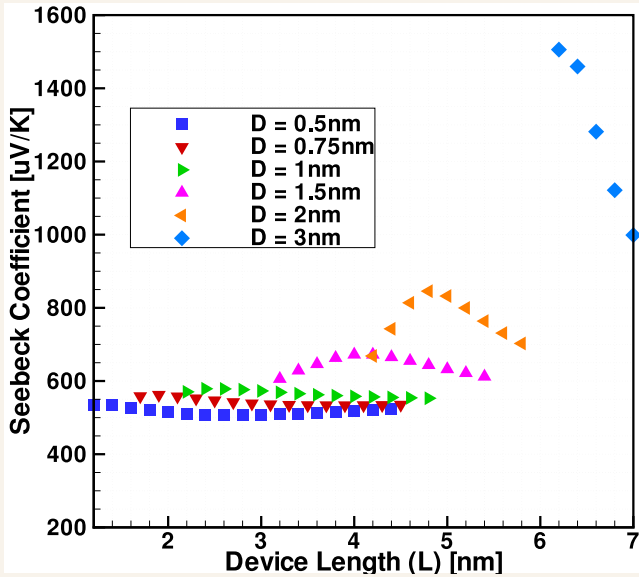
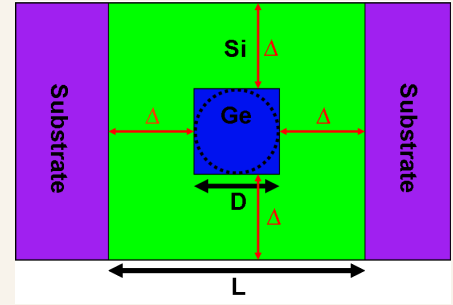


- Silicon Matrix, Germanium crystal has greatest Seebeck.
- Straining of the Silicon crystal results in degeneracy.

# Crystal Spacing Effects



- Maintain crystal diameter and increase spacing between nearest neighbor crystal.



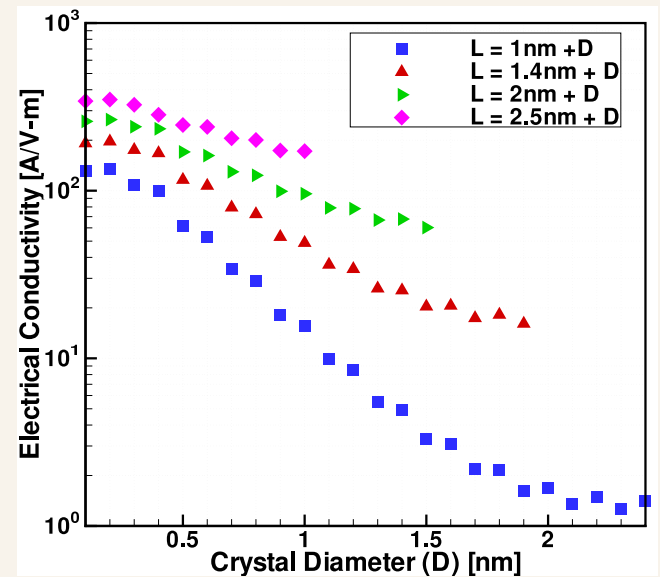
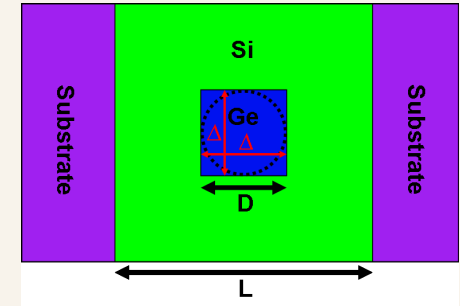
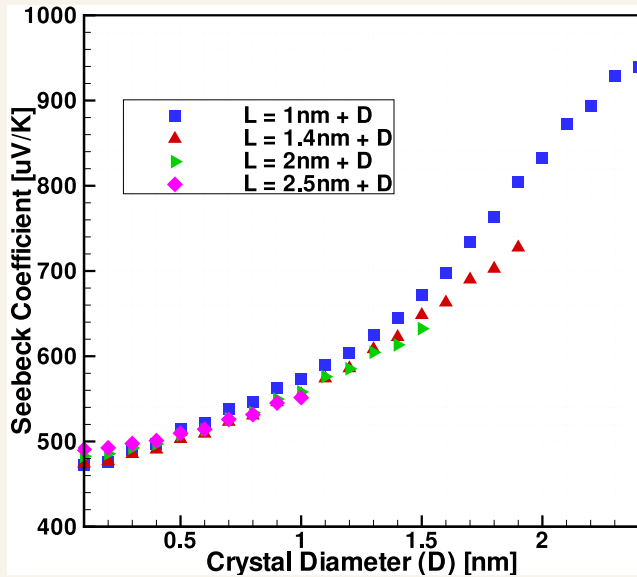
- Maximum in Seebeck is evident for larger crystals.
- Locus of optimal crystal spacing.



# Crystal Diameter Effects



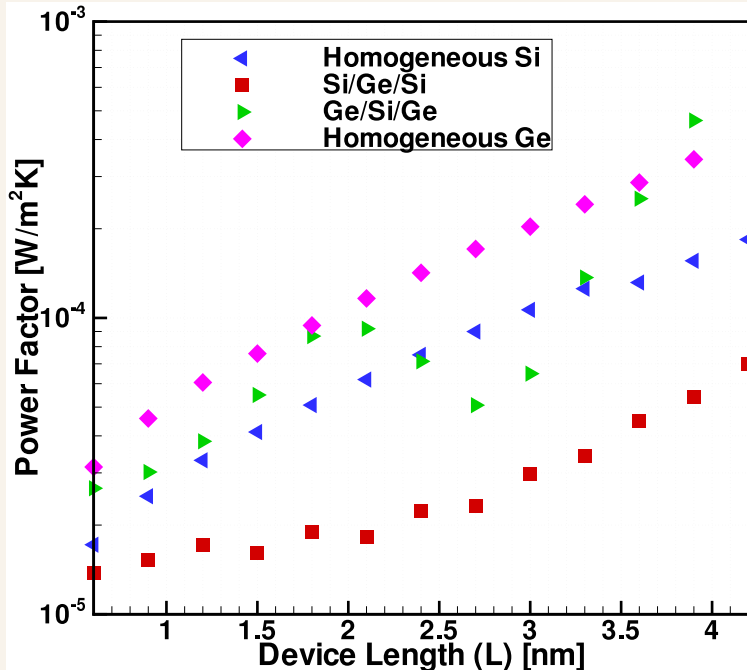
- Maintain crystal spacing and increase crystal diameter.



- Competing effects between Seebeck and Conductivity.

- Figure of Merit

$$ZT = \frac{S^2 \sigma T}{k} \quad (1)$$



- Homogeneous Ge proves to have greatest Power Factor.
- Ge/Si/Ge has greater power factor than Si/Ge/Si.
- Power Factor has strong dependence on electrical conductivity which can be controlled by parameters such as doping.



- Straining is a critical mechanism in electrical transport
- NCCs' have greater Seebeck than homogenous homogeneous Si
- Optimization of NCC Thermoelectric Devices
  - Greater Seebeck for silicon crystal in germanium matrix
  - Small crystal size preferred  $< 50\%$  device size
  - Crystal spacing in transport direction  $50\%$
  - Optimal Power Factor has yet to be determined based on device size.  $> 5\text{nm}$
- Further investigation of thermal conductivity is required to determine complete figure of merit.